

## Erratum

In Section 4 we defined two kinds of categorical models called  $\lambda_c 2_\eta$ -models and monadic  $\lambda_c 2_\eta$ -models, where the latter is stronger notion than the former; and in Theorem 4 we stated that the  $\lambda_c 2_\eta$ -calculus is sound and complete for the  $\lambda_c 2_\eta$ -models. It turns out that this does not hold, and instead we have to assume monadic  $\lambda_c 2_\eta$ -models rather than  $\lambda_c 2_\eta$ -models; this is necessary in the sense that the calculus is also complete for the monadic  $\lambda_c 2_\eta$ -models, as the term model becomes a monadic  $\lambda_c 2_\eta$ -model. Thus a correct theorem instead of Theorem 4 is:

**Theorem** *The  $\lambda_c 2_\eta$ -calculus is sound and complete with respect to the monadic  $\lambda_c 2_\eta$ -models.*  $\square$

What is overlooked in a proof of the soundness is the lemma that, for any value  $V$ , its interpretation  $\llbracket V \rrbracket$  is a value (i.e., in the image of the Kleisli embedding); its proof itself is straightforward by induction on  $V$  (once we assume monadic  $\lambda_c 2_\eta$ -models).

All the parts except for Theorem 4 in the paper are correct—where first of all we do not use the notion of  $\lambda_c 2_\eta$ -models (but use the stronger notion of monadic  $\lambda_c 2_\eta$ -models)—, especially including Sections 5 and 6 on construction of concrete monadic  $\lambda_c 2_\eta$ -models.

**Remark** *Once we apply the above erratum, we use only the notion of monadic  $\lambda_c 2_\eta$ -models and do not use that of  $\lambda_c 2_\eta$ -models at all; then it seems better to use the terminology  $\lambda_c 2_\eta$ -models for the notion of monadic  $\lambda_c 2_\eta$ -models, (though in this erratum we always use the terminology in the original paper to avoid confusion).*  $\square$